Diffie Hellman Example COMP830

Diffie Hellman is a Key exchange protocol designed to allow the sharing of a calculated symmetric key.

There are 2 people who do not know each other who wish to calculate the same secret (shared / symmetric) key. They must do this publicly where anyone listening can hear what they are communicating.

Alice tells Bob publicly her chosen prime number (q=7). (public)

Bob Tells Alice publicly his chosen prime number (a=5). (public)

They then choose secret keys that only they will know. They do not tell each other what this key is.

Alice selects: xa = 13 (private) Bob selects: xb = 17 (private)

 $Y_A = a^{xa} \mod q \Longrightarrow Y_A = 5^{13} \mod 7$ => $Y_A = 5^{13} (1220703125) \mod 7 \Longrightarrow Y_A = 5 (public)$

 $Y_B = a^{xb} \mod q \Longrightarrow Y_B = 5^{17} \mod 7$ => $Y_B = 5^{17} (762939453125) \mod 7 \Longrightarrow Y_B = 3$ (public)

Y_A is Alices's public key which she sends to Bob

 Y_B is Bob's public key which he sends to Alice.

They now calculate the shared symmetric key.

$$\begin{split} K_{AB} &= Y_B{}^{xa} \bmod q \Longrightarrow Y_B{}^{13} \bmod 7 \Longrightarrow 3{}^{13} \bmod 7 \Longrightarrow 1594323 \bmod 7 = 3 \\ K_{AB} &= Y_A{}^{xb} \bmod q \Longrightarrow Y_A{}^{17} \bmod 7 \Longrightarrow 5{}^{17} \bmod 7 \Longrightarrow 762939453125 \bmod 7 = 3 \end{split}$$

Their Shared Secret Key is 3.